## Notes for Lab 5 (Analog-to-Digital Converter (ADC) Lab)

## 1. This is *not* a lab on analog-to-digital conversion

- For a signal to be *digital*, it must have both a discrete (i.e., *countable*) domain (e.g., time) and range (e.g., values). Additionally, its range must be *finite*. Recall that you can use the *digits* of your hands (i.e., your *fingers*) to *count* a *finite* number of items.
  - Discrete-time analog signals can be generated by *sampling* continuous-time analog signals.
    - \* Each sample can have a *continuous* range of values.
    - \* For slow signals, sampling is *error free*.
  - A digital signal can be generated by *quantizing* (or *quantumizing*) each sample of a discrete-time analog signal.
    - \* A quantizer (or quantumizer) can only produce a finite number of outputs (e.g., 0–255).
      - $\cdot$  The outputs are called *codes*.
      - $\cdot$  So a quantizer encodes data.
      - $\cdot\,$  The resolution of the quantizer is the number of possible output values.
    - \* An analog-to-digital converter (ADC) is a quantizer.
      - $\cdot\,$  When designing ADCs, for a single  $\mathit{cost},$  there is a speed–resolution tradeoff.
    - \* A digital signal is an *estimate* of an analog signal, so it is subject to *estimation error*.
- Nyquist–Shannon *sampling* theorem
  - An analog signal that is sampled at *constant* intervals can be *accurately reconstructed* so long as the *range* of frequencies in the signal is small enough.
  - Sampling frequency must be *twice* the *bandwidth* of the signal.
  - To reconstruct original signal, *sinc interpolation* is used to fill-in time between samples.
  - This classical result has been used by *analog* engineers for years to do lots of useful things.
  - You should NOT associate "Nyquist" and "digital" in your head.
- Quantization noise floor
  - Quantization has two negative effects (that are really the same single effect).
    - (i) It limits the *dynamic range* (i.e., the maximum/minimum signal ratio) of signals.
      - \* To encode a signal that can be large, small variations (even if they are slow) will be lost completely.
    - (ii) It introduces quantization (or quantumization) noise and distortion.
      - \* It gives a continuous *range* of inputs a *single* identity (*round-off error*).
  - So quantization creates a *noise floor*. Characteristics smaller than "1 LSB" are lost.
    - \* "LSB" = "Least Significant Bit" = |input range|/resolution
    - \* Increase resolution to decrease LSB
  - Quantization noise *spectrum* can be *shaped* using *dither*.
    - \* When quantizing a value between two outputs, randomly choose to round up or down based on how close the value is to the nearest output.
    - $\ast\,$  For example, for outputs "0" and "1", encode "0.75" as "1" 75% of the time and "0" 25% of the time.
    - \* Reconstruction will involve a low-pass filter that will have an *averaging* effect.
    - \* Averaging effect *tilts* noise floor lower at low frequencies and higher at high frequencies.
    - Slow-changing signals have near-constant values that hit lots of sequential samples, so they get reconstructed perfectly.
      - $\cdot\,$  Fast-changing signals have values that only get one sample, which is now extra noisy. So reconstruction is bad.

- \* Amount of "tilt" is determined by sampling, so oversample too.
- \* 2D visual example (replace "time" with "space"): Red-to-white color gradient
  - $\cdot\,$  Discrete-time analog signal still shows "pink" in the middle.
  - · 1-bit quantization (i.e., *resolve* signal into 2 values) shows red half and white half.
  - $\cdot\,$  1-bit quantization with dither (and plenty of sampling) has "pixels." Pixels in middle are interlaced 50% red and 50% white. Eye filters them and sees pink.
- \* Dithered ADCs that oversample have high *signal-to-noise-and-distortion (SINAD)*, which gives them resolutions with high *effective number of bits (ENOB)*.
- Dithering methods
  - $\ast\,$  Add 1 LSB of uniform white noise to signal and always round resulting signal up.
    - $\cdot\,$  Values between two codes will be evenly balanced.
    - $\cdot\,$  Values closer to one code will have more conversions favoring that code.
  - \* Sigma-Delta (SD,  $\Sigma\Delta$ , Delta-Sigma, or  $\Delta\Sigma$ ) conversion pulse **density** modulation (PDM)
    - · Picture non-inverting op amp buffer (i.e., output shorted to inverting (-) input).
    - $\cdot\,$  Before feeding back output, insert clocked D flip–flop that outputs op amp rails.
    - · Negative feedback will cause average flip-flop (1-bit ADC) output to track the input.
    - $\cdot\,$  Counting output density (i.e., fraction of high outputs in a period of time) gives dithered conversion.
    - $\cdot\,$  Devices are **cheap** to make a 1-bit flash ADC is a simple comparator.
- Precision DMM's (i.e., > 6 digits) use  $\Sigma$ - $\Delta$  ADCs
  - \* Their inputs are slow (e.g., battery voltages).
  - \* For these slow inputs, they have fast conversion and very low quantization noise.
  - \* Precision DMM's are analog masterpieces.
- 2. The magic of pulses not limited to just  $\Sigma$ - $\Delta$  ADCs (note: same magic is behind "Class-D" amplifiers)
  - A *pulse* is a rapid change in a signal from one value to another.
    - For signals made entirely of pulses, time between two pulses is the "pulse width" of first pulse.
  - Discrete values are easy to generate, detect, and store.
    - Switches dissipate no power  $(i = 0 \text{ or } v = 0 \text{ so } i \times v = 0)$ .
      - \* A signal consisting of only high and low rail values can be generated with no dissipation.
      - \* Compare to analog amplifier that balances dissipation to move output.
    - Easy to detect "high" or "low" even with noise.
    - Easy to store (and read) "high" or "low" (e.g., "pits" and "lands" on CDs).
  - Continuous values can still be stored in time (e.g., widths of pulses).
    - Use "1-bit" resolution, detect *fast transitions*, and send continuous samples as *durations*.
      - \* Usually noise and distortion has a bigger impact on *value* than *time*.
    - Can convert to digital by *counting*. Resolution set by *clock*, and so it's programmable.
  - Examples: Flashlight communication from earth to mars; storing information on a CD

- 3. Today's lab: Transmission of analog signal via pulse widths
  - Pulse width modulation (PWM)
    - Transmitter pulses output high and low.
    - *Time* between a high and a low transition represents the *height* of a sample.
    - So each *pulse width* communicates a single *sample* of the signal.
    - Value-to-duration conversion is *modulation*. Duration-to-value conversion is *demodulation*.
    - A device that does both is a modem (i.e., a "mod"-"dem").
  - The output of this lab (the *modulator*) is an electrical signal.
    - That signal will drive an infrared transmitter so that we can communicate over the air (i.e., air as *communication channel*).
      - \* We will build this "IR-link" next week.
    - That signal *could* drive a CD burner so that we can communicate over CD (i.e., CD as communication channel).
    - The actual communication channel is *arbitrary*.
  - Ideal implementation with comparator
    - Place signal at one input and *comparison function* at the other
    - Comparison function converts values to durations (i.e., time)
      - \* Sweeps through entire input range
        - $\cdot\,$  Output pulses (switches) when inputs cross
        - $\cdot$  Intervals between samples are not constant (Nyquist implications?)
      - \* Several popular comparison functions
        - $\cdot$  555 datasheet uses decaying exponential (easy to generate from RC charging)
        - $\cdot$  Triangle wave is harder to generate, but is demodulated cleanly with low-pass filter
        - We use sawtooth-like ramp train (tradeoff) current source and capacitor (i = Cv')
- 4. Infrared link, hysteresis, and design constraints
  - Infrared signals are small and noisy
  - A simple infrared receiver will see many false transitions
    - Filter the output to make the transitions smooth
    - Use Schmitt trigger to toggle output only after smooth output reaches threshold
    - Hysteresis effect: transfer function depends on current state/history
  - So pulses must have  $6 \mu s$  between them to be detected; otherwise, trigger holds output constant
- 5. Our pulse-width modulator's parts:
  - (i) Level-shifter amplifier with  $\times 3$  gain and  $5 V_{\rm DC}$  offset
    - Continuous-time Input: Signal between -1 V and 1 V with  $0 V_{DC}$  offset
    - $\bullet\,$  Output sits between  $2\,\mathrm{V}$  and  $8\,\mathrm{V}$
  - (ii) Ramp generator with asynchronous reset
    - Constant current source driving capacitor load
    - Current and capacitance chosen to fix slope
    - Slope between  $(2 \text{ V})/(6 \mu \text{s})$  and  $(8 \text{ V})/(T 6 \mu \text{s})$ , where T is period of  $\sim 30 \text{ kHz}$  clock
    - Instantly resets to 0 V when reset signal asserted
  - (iii) Comparator (i.e., an "ideal" PWM does the sampling)
  - (iv)  $\sim 30 \text{ kHz}$  clocked flip–flop with asynchronous reset
    - **Output**: Pulse train with widths modulated by discrete-time samples of input



- 6. Our PWM operation:
  - At every *rising edge* of the clock:
    - (i) Modulator output (i.e., flip-flop's Q) transitions from low to high
    - Flip-flop clocks in a "1" from synchronous input(ii) Ramp resets to 0 V and *starts rising* 
      - Its own (asynchronous) reset is tied to  $\overline{Q}$ , which goes low
  - Whenever comparator detects that ramp rises *above* input, asynchronously resets flip-flop
    - High output Q goes low
    - Ramp resets because  $\overline{Q}$  goes high
      - $\ast\,$ Ramp doesn't rise until next clock
      - \* So only one sample per clock cycle
  - $\bullet\,$  Shift and amplify input so that it stays within  $2\,\mathrm{V}$  and  $8\,\mathrm{V}\,$
  - Set ramp slope to meet  $6 \,\mu s$  hysteresis constraints
    - (i) Ramp takes at least 6  $\mu$ s to hit 2 V (slope  $\leq (2/6) V/\mu s \approx 0.333 V/\mu s$ )
    - (ii) Ramp hits 8 V with 6  $\mu$ s or more before next clock edge (slope  $\geq (8 \text{ V})/(T 6 \mu \text{s}))$ - T is your clock's period
  - Note that comparator and flip-flop could be implemented with a single 555 timer IC
  - Note that intervals between samples are **not** constant (distortion? Nyquist consequences?)
- 7. Parts in the lab
  - Use CD4027 JK flip-flop with asynchronous set-reset (SR)
    - Clock transitions bring output high, so
      - \* Connect J high
      - \* Connect K low
    - Comparator brings output low, so
      - \* Connect S low
      - \* Connect comparator to R
  - Use LM311 voltage comparator with **open-collector** output
    - Output is the **floating collector** of a *npn* common-emitter amplifier acting as "BJT switch"
    - Output requires *pull-up resistor* (e.g.,  $1 \text{ k}\Omega$ ) for operation (otherwise, output cannot go high)
    - Comparator pin-out very different from op. amp.: be sure to use the right pin-out
      - \* Uses all three  $V_{CC},\,V_{EE},\,\text{and }GND$  (tie both  $V_{EE}$  and GND to 0 V)
      - $\ast\,$  Inputs are still on pins 2 and 3, but they are swapped
      - \* Other similar inputs/outputs on completely different pins

- 8. Laboratory experience
  - Many design alternatives given
  - Remember your ramp slope
    - You will need to build a second ramp generator for the demodulator
    - The two ramp slopes must match
  - Make use of **bypass capacitors** at *supply pins* to reduce output noise
  - When taking plots, save as CSV or BMP
    - Saving as BMP prevents extra work, but make sure scope plots show all required information
      - $\ast\,$  Intervals between horizontal and vertical divisions should be clear
      - $\ast\,$  In most cases, channel grounds should be shown
      - \* Channels should be labeled in report (e.g., "top waveform is input")
    - If saving as CSV, be sure to...
      - \* Label axes and show units
      - \* Identify waveforms (e.g., "input" and "output")
  - See pin-out handout
    - Important difference between OA and comparator pin-outs
  - Follow lab *book* procedures
    - Handout gives detailed instructions
    - In part 2, give slopes in  $V/\mu$ s units
    - Keep resulting **pulse-width modulator** for future labs
- 9. Laboratory reports
  - Answer all questions and provide all plots from lab procedures in lab text
  - Include ALL PLOTS from procedure (even if they aren't mentioned in book)
    - USE the plots in your discussion
  - Consider answering some of the questions from the procedure